

GUJARAT UNIVERSITY
B.E. SEM – 3 (CIVIL/ENV)
Question Bank
Applied Maths – II

Each question is of equal Marks (10 Marks)

Q.1	Find the Fourier Series for $f(x) = e^{-x}$ in the interval $0 < x < 2\pi$.
Q.2	Expand $f(x) = x \sin x$ as a Fourier series in the interval $0 < x < 2\pi$.
Q.3	Find the Fourier series of $f(x) = 2x - x^2$ in the interval $(0,3)$. Hence deduce that $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \dots = \frac{\pi^2}{12}$.
Q.4	Find the Fourier series of the function $f(x) = \begin{cases} x^2 & 0 \leq x \leq \pi \\ -x^2 & -\pi \leq x \leq 0 \end{cases}$.
Q.5	Find the Fourier series of the function $f(x) = \begin{cases} \pi x & 0 < x < 1 \\ 0 & x = 1 \\ \pi(x-2) & 1 < x < 2 \end{cases}$. Hence show that $\frac{1}{1} - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{\pi}{4}$.
Q.6	Find the Fourier series of $f(x) = x^2$ in the interval $0 < x < a$, $f(x+a) = f(x)$.
Q.7	If $f(x) = \cos x $, expand $f(x)$ as a Fourier series in the interval $(-\pi, \pi)$, $f(x+2\pi) = f(x)$.
Q.8	For the function $f(x)$ defined by $f(x) = x $, in the interval $(-\pi, \pi)$. Obtain the Fourier series. Deduce that $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$.
Q.9	Given $f(x) = \begin{cases} -x+1 & -\pi \leq x \leq 0 \\ x+1 & 0 \leq x \leq \pi \end{cases}$. Is the function even or odd? Find the Fourier series for $f(x)$ and deduce the value of $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$.
Q.10	Find the Fourier series of the periodic function $f(x)$; $f(x) = -k$ when $-\pi < x < 0$ and $f(x) = k$ when $0 < x < \pi$, and $f(x+2\pi) = f(x)$.
Q.11	Half range sine and cosine series of $f(x) = x(\pi - x)$ in $(0, \pi)$
Q.12	Find the Fourier series for the function $f(x) = \begin{cases} \pi x, 0 < x < 1 \\ \pi(x-2), 1 < x < 2 \end{cases}$
Q.13	Find the Fourier series for $f(x)$ defined by $f(x) = x + \frac{x^2}{4}$ when $-\pi < x < \pi$ and $f(x+2\pi) = f(x)$ and hence show that $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$
Q.14	Find the Fourier series for the function $f(x) = \begin{cases} x; 0 < x < 1 \\ 0; 1 < x < 2 \end{cases}$.

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Q.15	<p>If $f(x) = x$ in $0 < x < \frac{\pi}{2}$</p> <p style="padding-left: 40px;">$= \pi - x$ in $\frac{\pi}{2} < x < \frac{3\pi}{2}$</p> <p style="padding-left: 40px;">$= x - 2\pi$ in $\frac{3\pi}{2} < x < 2\pi$</p> <p>Prove that $f(x) = \frac{4}{\pi} \left\{ \frac{\sin x}{1^2} - \frac{\sin 3x}{3^2} + \frac{\sin 5x}{5^2} - \dots \right\}$</p>
Q.16	<p>If $f(x) = \frac{x}{l}$ when $0 < x < l$</p> <p style="padding-left: 40px;">$= \frac{2l-x}{l}$ when $l < x < 2l$</p> <p>Prove that $f(x) = \frac{1}{2} - \frac{4}{\pi^2} \left(\frac{1}{1^2} \cos \frac{\pi x}{l} + \frac{1}{3^2} \cos \frac{3\pi x}{l} + \frac{1}{5^2} \cos \frac{5\pi x}{l} + \dots \right)$</p>
Q.17	<p>When x lies between $\pm\pi$ and p is not an integer, prove that</p> $\sin px = \frac{2}{\pi} \sin p\pi \left(\frac{\sin x}{1^2 - p^2} - \frac{2 \sin 2x}{2^2 - p^2} + \frac{3 \sin 3x}{3^2 - p^2} - \dots \right)$
Q.18	Find the Fourier series for the function $f(x) = e^{ax}$ in $(-l, l)$
Q.19	Half range sine and cosine series of $f(x) = 2x - 1$ in $(0, 1)$
Q.20	Half range sine and cosine series of x^2 in $(0, \pi)$
Q.21	Find Half range sine and cosine series for $f(x) = (x - 1)^2$ in $(0, 1)$
Q.22	Evaluate: $L\{\sin 2t \cos 3t\}$, $L\{e^{-3t}(\cos 4t + \sin 2t)\}$
Q.23	Evaluate: $L\{\sin^2 2t\}$, $L\{e^{-2t} \cos 3t\}$

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Q.24	Evaluate: $L\left\{\frac{\sin 2t - \sin 3t}{t}\right\}$, $L\left\{t \int_0^t e^{-4t} \sin 3tdt\right\}$
Q.25	Evaluate: $L^{-1}\left\{\log\left(\frac{s+1}{s-1}\right)\right\}$, $L^{-1}\left\{\frac{s^2 + s + 2}{s^5}\right\}$
Q.26	Evaluate: $L^{-1}\left\{\cot^{-1}\frac{s}{a}\right\}$, $L^{-1}\left\{\frac{s-1}{(s-1)^2 + 4}\right\}$
Q.27	Evaluate: $L^{-1}\left\{\log\left(\frac{s+2}{s+3}\right)\right\}$, $L^{-1}\left\{\frac{s+2}{(s^2 + 4s + 5)^2}\right\}$
Q.28	Evaluate: $L^{-1}\left\{\frac{1+2s}{(s+2)^2 (s-1)^2}\right\}$, $L^{-1}\left\{\frac{s^2 + s + 3}{s^6}\right\}$
Q.29	Evaluate: $L^{-1}\left\{\frac{(s+1)^2}{s^3}\right\}$, $L^{-1}\left\{\tan^{-1}\frac{s}{a}\right\}$
Q.30	Find the Laplace Transform of f(t), where $(i) f(t) = \begin{cases} t & \text{if } 0 < t < \frac{a}{2}, \\ a - t & \text{if } \frac{a}{2} < t < a \end{cases}, \quad f(t+a) = f(t)$
Q.31	Find the Laplace transform of the function $f(t) = \begin{cases} \sin \omega t; 0 < t < \frac{\pi}{\omega} \\ 0; \frac{\pi}{\omega} < t < \frac{2\pi}{\omega} \end{cases}, \quad f(t) = f\left(t + \frac{2\pi}{\omega}\right)$
Q.32	Use convolution theorem to find the Laplace Inverse Transform of $(i) \frac{sa}{(s^2 - a^2)^2} \quad (ii) \frac{s-2}{s(s-4s-13)}$
Q.33	Use convolution theorem to find the Laplace Inverse Transform of

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	(i) $\frac{s^2}{(s^2 + a^2)(s^2 - b^2)}$ (ii) $\frac{1}{s^2(s-2)}$
Q.34	Find the value of the integral using Laplace Transform technique. (i) $\int_0^{\infty} t e^{-2t} \cos t dt$ (ii) $\int_0^t e^{-t} \frac{\sin t}{t} dt$
Q.35	Solve the initial value problem $y'' + 5y' + 2y = e^{-2t}$, $y(0) = 1$, $y'(0) = 1$, Using Laplace transformation.
Q.36	Solve the following Differential Equations using Laplace Transform technique. $\frac{d^2x}{dt^2} - 2 \frac{dx}{dt} + x = e^t$ with $x = 2$ and $\frac{dx}{dt} = -1$ at $t = 0$
Q.37	Solve the following Differential Equations using Laplace Transform technique. $\frac{d^2y}{dx^2} + y = 1$ with $y(0) = 1$ and $y\left[\frac{\pi}{2}\right] = 0$
Q.38	Solve the following equations : (a) $(D - 2)^2 y = 8(e^{2x} + \sin 2x + x^2)$ (b) $(D^2 + D) y = x^2 + 2x + 4$
Q.39	Solve the following equations : (a) $(D^2 + 1) y = x^2 \cos x$ (b) $(D^2 + 1) y = e^{2x} + \cosh 2x + x^3$
Q.40	Solve the following equations : (a) $(D^4 + 2D^2 + 1) y = x^2 \cos^2 x$ (b) $(D^2 + 2) y = e^{-2x} + \cos 3x + x^2$
Q.41	Solve the following equations : (a) $(D^2 + 2D + 1) y = x e^x \sin x$ (b) $(D^2 - 9) y = e^{3x} \cos 2x$
Q.42	Solve the following equations : (a) $(D - 2)^2 y = 8(e^{2x} + \sin 2x + x^2)$ (b) $(D^3 + 8) y = x^4 + 2x + 1$
Q.43	Solve the following equations :

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	(a) $(D^2 - 1)y = x \sin 3x + \cos x$ (b) $(D^2 - 4D + 4)y = 2e^x + \cos 2x + x^3$
Q.44	Solve: $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 5y = x^2 \sin(\log x)$.
Q.45	Solve: $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + y = ((\log x) \sin(\log x) + 1) / x$
Q.46	Solve: $(3x + 2) \frac{d^2 y}{dx^2} + 3(3x + 2) \frac{dy}{dx} - 36y = 3x^2 + 4x + 1$.
Q.47	Solve: $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 5y = x^2 \sin(\log x)$.
Q.48	Solve: $x^2 \frac{d^2 y}{dx^2} - 2x \frac{dy}{dx} - 4y = x^2 + 2 \log x$.
Q.49	Solve by using method of variation of parameters: $\frac{d^2 y}{dx^2} + y = \sec x$.
Q.50	Solve by using method of variation of parameters: $\frac{d^2 y}{dx^2} + y = \tan x$.
Q.51	Solve by using method of variation of parameters: $\frac{d^2 y}{dx^2} - 2 \frac{dy}{dx} = e^x \sin x$
Q.52	The charge q on a plate of a condenser C is given by $L \frac{d^2 q}{dt^2} + R \frac{dq}{dt} + \frac{q}{c} = E \sin pt$ the circuit is tuned to resonance so that $p^2 = \frac{1}{LC}$ if initially the current i and charge q be zero show that for small value of $\frac{R}{L}$, the current in the circuit at time t is given by $\left(\frac{Et}{2L}\right) \sin pt$.
Q.53	Solve the following simultaneous equations: $Dx + y = \sin t$ $Dy + x = \cos t$; where $D = \frac{d}{dt}$

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	given that when $t=0$, $x=1$ and $y=0$.
Q.54	Solve the following simultaneous equations: $Dx + y = e^t$ $Dy + x = e^{-t}$; where $D = \frac{d}{dt}$
Q.55	Form the partial differential equation of following: (a) $2z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$ (b) $z = f(x+ct) + g(x-ct)$
Q.56	Form the partial differential equation of following: (a) $2z = a^2x^2 + b^2y^2$ (b) $z = x + y + f(xy)$
Q.57	Form the partial differential equation of following: (a) $z = (x^2 + a)(y^2 + b)$ (b) $F(xy+z^2, x+y+z) = 0$
Q.58	Solve following partial differential equations : (a) $x(y^2 - z^2)p + y(z^2 - x^2)q = z(x^2 - y^2)$ (b) $x(y-z)p + y(z-x)q = z(x-y)$
Q.59	Solve following partial differential equations : (a) $py + qx = pq$ (b) $z = px + qy + 2\sqrt{pq}$
Q.60	Solve following partial differential equations : (a) $\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial x \partial y} = \sin x \cos y + xy$ (b) $\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial x \partial y} = \cos x \cos 2y$
Q.61	Solve following partial differential equations : (a) $\frac{\partial^2 z}{\partial x^2} - 2 \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = e^{x+4y}$ (b) $\frac{\partial^2 z}{\partial x^2} - 2 \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = x^3 + e^{x+2y}$
Q.62	(a) Solve: $\frac{\partial^2 z}{\partial x \partial y} = e^{-y} \cos x$, given that $z = 0$ when $y = 0$ and $\frac{\partial z}{\partial y} = 0$ when $x = 0$ (b) Solve: $\frac{\partial^2 z}{\partial x^2} = z$ given that $z = e^y$ and $\frac{\partial z}{\partial x} = e^{-y}$ when $x = 0$

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Q.63	Solve: $\frac{\partial z}{\partial x} = 2 \frac{\partial z}{\partial y} + z$ where $z(x, 0) = 8 e^{-5x}$ using method of separation of variables.
Q.64	Solve: $3 \frac{\partial z}{\partial x} + 2 \frac{\partial z}{\partial y} = 0$, where $z(x, 0) = 4 e^{-x}$ by using method of separation of variables.
Q.65	Solve: $\frac{\partial z}{\partial x} = 4 \frac{\partial z}{\partial y}$ where $z(0, y) = 8 e^{-3y}$ using method of separation of variables.
Q.66	(a) Find real root of the equation $x^3 + x^2 + 1 = 0$ by using method of direct iteration correct up to three decimal places. (b) By using Newton –Raphson’s get the real root of the equation $xe^x - 2 = 0$ correct up to two decimal places
Q.67	(a) Find the real root of the equation $x \log_{10} x - 1.2 = 0$ by false position method. (b) By using Newton –Raphson’s get the real root of the equation $x = e^{-x}$ near $x = 0.5$ correct up to two decimal places.
Q.68	(a) Using the method of iteration, find the roots of the equation $x^4 - 3x + 1 = 0$ $x_0 = 1.5$ correct to four decimal places. (b) Find a root of the equation $x^3 - x - 1 = 0$ correct to three decimal places, using the bisection method.
Q.69	(a) Find root of the equation $xe^x = \cos x$ correct to three decimal places using method of False-position. (b) Find root of the equation $x^3 - 3x + 5 = 0$ correct to three decimal places using method of Newton-Raphson.